Chapter 6: More advanced exercises

You will find in this tutorial a collection of more advanced exercises. You might also want to have a look at the worksheets on "Collatz conjecture", "Dictionaries and graph theory" and "Strings and the Burrows-Wheeler transform".

Exercise 6.1

How many strings of length *n* containing only letters a and b but not containing a are there? Compute the value for each n = 1, 2, ..., 10

Do you know this sequence?

Could you find the corresponding entry in the OEIS

Exercise 6.2 (Goldbach conjecture)

Verify experimentally the following statement: « For each even integer $n \ge 4$, there exist two prime number $p \ge 2$ and $q \ge 2$ such that n = p + q ».

Up to which value of *n* are you able to verify this conjecture?

Exercise 6.3

Does there exist two positive integer numbers x and y such that $x^2 - 61y^2 = 1$?

Exercise 6.4

Write a function that given positive integers (p,q,n) return the number of solutions in positive integers (a_1,a_2,\ldots,a_n) to the equation

$$\frac{1}{a_1} + \frac{1}{a_2} + \ldots + \frac{1}{a_n} = \frac{p}{q}$$

How many solutions are there for (p,q,n) = (13,12,3)?

A sample of Euler problems

Solve the following Euler problems

- problem 26 (decimal expansions)
- problem 31 (coin sums)

- problem 45 (triangular, pentagonal and hexagonal numbers)
- problem 46 (odd composite number that can not be written as the sum of a prime and twice a square)
- problem 50 (sum of consecutive primes that are primes)