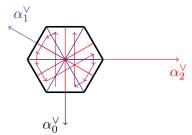
The Sage system

Nicolas M. Thiéry

With slides from Franco Saliola, Florent Hivert, Dan Drake, William Stein, ...

Laboratoire de Mathématiques d'Orsay, Université Paris Sud

Sage Days 28, Orsay, 17/01/2011



Sage's mission

"To create a viable high-quality and open-source alternative to $Maple^{TM}$, $Mathematica^{TM}$, $Magma^{TM}$, and $MATLAB^{TM}$

٠.

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"To create a viable high-quality and open-source alternative to Maple TM , Mathematica TM , Magma TM , and MATLAB TM

. . .

and to foster a friendly community of users and developers"

Sage's design principles

- Developed by a community of users, for users
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 Atlas, GAP, GMP, Linbox, Maxima, MPFR, PARI/GP,
 NetworkX, NTL, Numpy/Scipy, Singular, Symmetrica, ...
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- Bazaar development model
- Active proselytism

A short history of Sage

- 2002: Open Source Computer Algebra workshop in Lyon
- 1999-2005: William Stein writes over 25,000 lines of Magma code for his research, and realizes that Magma was a bad long term investment since he couldn't see or modify the internals
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- Feb. 2010: Sage 4.4.2 Sage Days 20, Luminy (France), 120 participants
- Jan. 2011: Sage 4.6.1
- 10000 users?
- Funding (postdoc, workshops, hardware): NSF, ANR, CNRS, Universities and Institutes, Google, Microsoft Research, ...

Sage is very young!

Sage has:

- bugs
- inconsistencies
- blank or undocumented areas

Sage lacks:

- native support under Windows (upcoming)
- (working) packages under Debian / Ubuntu / ...
- Proper modularization

```
ATLAS
                Automatically Tuned Linear Algebra Software
        BLAS
                Basic Fortan 77 linear algebra routines
        Bzip2
                High-quality data compressor
       Cddlib
                Double Description Method of Motzkin
Common Lisp
                Multi-paradigm and general-purpose programming lang.
    CVXOPT
                Convex optimization, linear programming, least squares
      Cython
                C-Extensions for Python
          F2c
                Converts Fortran 77 to C code
         Flint
                Fast Library for Number Theory
       FpLLL
                Euclidian lattice reduction
    FreeType
                A Free, High-Quality, and Portable Font Engine
```

G95 Open source Fortran 95 compiler GAP Groups, Algorithms, Programming GD Dynamic graphics generation tool Genus2reduction Curve data computation Gfan Gröbner fans and tropical varieties Givaro C++ library for arithmetic and algebra **GMP** GNU Multiple Precision Arithmetic Library GMP-ECM Elliptic Curve Method for Integer Factorization GNU TLS Secure networking GSL Gnu Scientific Library JsMath JavaScript implementation of LaTeX

IML Integer Matrix Library **IPython** Interactive Python shell LAPACK Fortan 77 linear algebra library Lcalc I -functions calculator Libgcrypt General purpose cryptographic library Libgpg-error Common error values for GnuPG components Linbox C++ linear algebra library Matplotlib Python plotting library Maxima computer algebra system Mercurial Revision control system Moin Moin Wiki

MPFI Multiple Precision Floating-point Interval library **MPFR** C library for multiple-precision floating-point computations **ECLib** Cremona's Programs for Elliptic curves NetworkX Graph theory NTI Number theory C++ library Numerical linear algebra Numpy OpenCDK Open Crypto Development Kit PALP A Package for Analyzing Lattice Polytopes PARI/GP Number theory calculator Pexpect Pseudo-tty control for Python PNG Bitmap image support

PolyBoRi Polynomials Over Boolean Rings PvCrypto Python Cryptography Toolkit Python Interpreted language Qd Quad-double/Double-double Computation Package R Statistical Computing Readline Line-editing Python interface to R Rpy Scipy Python library for scientific computation Singular fast commutative and noncommutative algebra Software construction tool Scons SQLite Relation database

Sympow L-function calculator Symmetrica Representation theory Sympy Python library for symbolic computation Tachyon lightweight 3d ray tracer Termcap for writing portable text mode applications Twisted Python networking library Weave Tools for including C/C++ code within Python Zlib Data compression library ZODB Object-oriented database

... and more!

Arbitrary precision arithmetic Algebra Algebraic geometry

Arithmetic geometry
Symbolic computation
Exact linear algebra
Numerical calculations
Combinatorics
Graph theory
Group theory

GAP, Maxima, Singular
Singular, Macaulay2 (optionnel)
GMP, MPFR, MPFI, NTL, ...
PARI, NTL, mwrank, ecm, ...
Maxima, Sympy
Linbox, IML
GSL, Scipy, Numpy
Symmetrica, Lrcalc, PALP, Coxe
NetworkX, graphviz (optional)
GAP

... and more!

> sage -gap

```
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Information at: http://www.gap-system.org
Try '?help' for help. See also '?copyright' and '?authors'

Loading the library. Please be patient, this may take a while. GAP4, Version: 4.4.10 of 02-0ct-2007, $x86_64$ -unknown-linux-gnu-gcc

> sage -singular

```
SINGULAR / Development

A Computer Algebra System for Polynomial Computations / version 3-1-0

by: G.-M. Greuel, G. Pfister, H. Schoenemann \ Mar 2009

FB Mathematik der Universitaet, D-67653 Kaiserslautern >
```

> sage -maxima

```
Maxima 5.16.3 http://maxima.sourceforge.net
Using Lisp ECL 9.4.1
Distributed under the GNU Public License. See the file COPYING.
Dedicated to the memory of William Schelter.
The function bug_report() provides bug reporting information.
(%i1)
```

> sage -gp

```
GP/PARI CALCULATOR Version 2.3.3 (released)
amd64 running linux (x86-64/GMP-4.2.1 kernel) 64-bit version
compiled: Jul 10 2009, gcc-4.3.2 (Ubuntu 4.3.2-1ubuntu12)
(readline v5.2 enabled, extended help available)
```

```
Copyright (C) 2000-2006 The PARI Group
```

PARI/GP is free software, covered by the GNU General Public License, and comes WITHOUT ANY WARRANTY WHATSOEVER.

```
Type ? for help, \q to quit.

Type ?12 for how to get moral (and possibly technical) support.

parisize = 8000000, primelimit = 500000
```

> sage -R

```
R version 2.6.1 (2007-11-26)
Copyright (C) 2007 The R Foundation for Statistical Computing
ISBN 3-900051-07-0
```

R is free software and comes with ABSOLUTELY NO WARRANTY. You are welcome to redistribute it under certain conditions. Type 'license()' or 'licence()' for distribution details.

Natural language support but running in an English locale

R is a collaborative project with many contributors.

Type 'contributors()' for more information and 'citation()' on how to cite R or R packages in publications.

Type 'demo()' for some demos, 'help()' for on-line help, or 'help.start()' for an HTML browser interface to help. Type 'q()' to quit R.

Sage combines the power of multiple software

Sage includes a large *native library*

- 500k lines of code
- 2500 classes
- 27058 functions
- Rich mathematical content: categories, combinatorics, graphs, number theory, ...
- Many new algorithms

Python is an interpreted multiparadigm programming language

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• Easy to use as a pocket calculator:

python: x = 17

python: x

17

python: 3*x

51

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Easy to read and write:

```
math: \left\{17x \mid x \in \{0,1,\ldots,9\} \text{ and } x \text{ is odd}\right\}
python: [17*x \text{ for } x \text{ in range}(10) \text{ if } x\%2 == 1]
```

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```

- Easy to learn, with lots of free documentation:
 - Dive into Python (http://diveintopython.adrahon.org)
 - Python tutorial(http://www.ceramiko.ch/python/main.html)

Python is a widely used language:

• One of the top 5 most used programming languages, with millions of programmers

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- *Cython*: code Python \longleftrightarrow code C.

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- Python is becoming a de facto standard for scientific computing

Sage is completely free

"You can read Sylow's Theorem and its proof in Huppert's book in the library . . . then you can use Sylow's Theorem for the rest of your life free of charge, but for many computer algebra systems license fees have to be paid regularly

With this situation two of the most basic rules of conduct in mathematics are violated: In mathematics information is passed on <u>free</u> of charge and everything is laid <u>open</u> for checking."

— J. Neubüser (1993) (started GAP in 1986) age? Python **Freedom!** Community Development mode

Freedom of execution

Anywhere, anytime, for any purpose, with only law as limit

Freedom to redistribute copies

or even to *sell* copies

Advantages:

- Technical and administrative simplicity
- Usage by students at home
- Remote computing, large scale calculations
- Sharing of your programs, worksheets
- Non discrimination
- Free access for non academic
- Free access for developing countries

Freedom of study

Advantages:

- Teaching
- Dissemination of science
- Most useful if the code is expressive!
- Reproducibility of scientific results
- Proof checking
- Control over the hypothesis, models and algorithms
- Analysis of bugs and unexpected behavior

Freedom to improve and publish one's improvements

Advantages:

- Adaptation to local needs (dialects, conventions)
- Specific developments
- Bug fixes
- Empowering of users
- Mutualisation of efforts
- Importance of communities

Sage's worldwide community



There currently are 184 contributors in 118 different places.

Python Community

Sage's worldwide community

```
web sites
    http://www.sagemath.org/
    http://www.sagemath.fr/
mailing lists
    sage-devel: development
    sage-windows: Windows port
    sage-release: release management
    sage-algebra: algebra
    sage-combinat-devel: combinatorics
    sage-finance finance
    sage-nt number theory
    sage-grid grid computing
    sage-edu teaching
    sagemath-edu teaching (in French)
```

irc-channel

#sage-devel on freenode.net

Sage Days!

- Intensive five days workshops (10-120 participants)
 Attract new users and developers
 Develop new features
- Introductory talks, tutorials
- Plenary conferences from computational experts
- Design brainstorms
- Coding sprints!

Sage Days in 2010

- Sage Days 19: Seattle, WA (January 2010)
- Sage Days 20: Marseille (February 2010)
- Sage Days 20.25: Montreal (March 2010)
- Sage Days 20.5: Fields Institute (May 2010)
- Sage Days 21: Seattle, WA (June 2010)
- Sage-Combinat/Chevie Workshop: France (June 2010)
- Sage Days 22: Berkeley, CA (July 2010)
- Sage Days 23: Leiden, Netherlands (July 2010)
- Sage Days 23.5: Kaiserslautern, Germany (July 2010)
- Sage Days 24: Linz, Austria (July 2010)
- Sage Days 25: Mumbai, India (August 2010)
- Sage Days 25.5 Montréal, Canada (September 2010)
- Sage Days 26 Seattle, Washington (December 7-10, 2010)

nge? Python Freedom! Community Development model

Some open source books!

• Calcul Mathématique avec Sage

Alexandre Casamayou, Guillaume Connan Thierry Dumont, Laurent Fousse François Maltey, Matthias Meulien Marc Mezzarobba, Clément Pernet Nicolas M. Thiéry, Paul Zimmermann

http://sagebook.gforge.inria.fr/ July 2010: 1.0 online August 2011: printed

Follow up to: Calcul formel, mode d'emploi Dumas, Gomez, Salvy, Zimmermann

- The Sage tutorial
 David Joyner, William Stein et al.
- A First Course in Linear Algebra Robert Beezer

High-quality code and documentation

All new code is:

- rigorously tested
- well documented
- peer-reviewed

```
> sage -coverage
```

Overall weighted coverage score: 81.1%

Total number of functions: 27058

We need 1061 more function to get to 85% coverage.

We need 2414 more function to get to 90% coverage.

We need 3767 more function to get to 95% coverage.

Development cycle

```
http://trac.sagemath.org/
```

Tickets (examples: #8154, #8890)

Patchs

New releases every 2-3 weeks

A typical computation in algebraic combinatorics involves

- A bit of standard combinatorics
- A bit of standard linear algebra
- A bit of standard group theory
- A bit of standard computer algebra
- A bit of standard ...

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- And that thin layer of your own magic powder

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But can 1?

*-Combinat: it all started there



*-Combinat: 1

Nicolas 20k

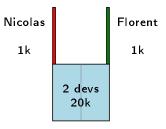
$$*-Combinat: 1+1 =$$

Nicolas 20k Florent 20k

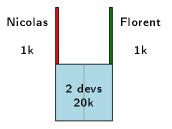
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*-Combinat:
$$1+1 = 1.1$$

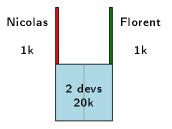


*-Combinat:
$$1+1 = 1.1$$



• 95% of development effort are generic

*-Combinat:
$$1+1 = 1.1$$



- 95% of development effort are generic
- Opportunity for sharing and mutualisation

http://mupad-combinat.sf.net http://combinat.sagemath.org

Mission statement: "To improve MuPAD/Sage as an extensible toolbox for computer exploration in combinatorics, and foster code sharing among researchers in this area"

- MuPAD: 115k lines of MuPAD, 15k lines of C++, 32k lines of tests, 600 pages of doc
- Sage: 300 tickets / 100k lines integrated in Sage
- Sponsors: ANR, PEPS, NSF, Google Summer of Code

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- A community:

Nicolas Borie, Daniel Bump, Jason Bandlow, Adrien Boussicault, Frédéric Chapoton, Vincent Delecroix, Paul-Olivier Dehaye, Tom Denton, François Descouens, Dan Drake, Teresa Gomez Diaz, Valentin Feray, Mike Hansen, Ralf Hemmecke, Florent Hivert, Brant Jones, Sébastien Labbé, Yann Laigle-Chapuy, Éric Laugerotte, Patrick Lemeur, Andrew Mathas, Xavier Molinero, Thierry Monteil, Olivier Mallet, Gregg Musiker, Jean-Christophe Novelli, Janvier Nzeutchap, Steven Pon, Viviane Pons, Franco Saliola, Anne Schilling, Mark Shimozono, Christian Stump, Lenny Tevlin, Nicolas M. Thiéry, Justin Walker, Qiang Wang, Mike Zabrocki, ...

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*-Combinat

1 1

> *-Combina[.] 15 devs 100k

MuPAD-Combinat : limits of the model

Me
1
1k

MuPAD-Combinat
15 devs
100k

MuPAD
15 devs
1M

Me 1 1k

Sage-Combinat 25 devs 100k

Sage 200 devs 1M Me
1
1k

Sage-Combinat
25 devs
100k

Sage
200 devs
1M

GAP, Maxima, Singular, ...
2M

Me 1k Sage-Combinat 25 devs 100k GAP, Maxima, Singular, ... Sage 200 devs 1M 2M SciPi, NumPi, Scientific Python, Atlas, Linbox, GMP, Matplotlib, JMOL, JSMath, ... 1k devs 10M

```
Me
 Sage-Combinat
  25 devs
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1k devs
10 M
```

Python, IPython, Firefox, Ajax, OpenGL, ...

1M dews

On the shoulders of a giant

```
Me
 Sage-Combinat
  25 devs
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