## Sage Days 23.5: Singular projects

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Vice versa,  $\operatorname{Singular}$  's partners will benefit from collaboration.

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- I SINGULAR's code for polynomial factorization is also used by MACAULAY2.
- 2 SINGULAR's ties with AIMS at Cape Town will contribute to spreading computer algebra throughout Africa.

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We believe that the further development of  $\mathrm{SAGE}$  will also be important to SPP1489. In this context, we are interested in  $\mathrm{SAGE}$ -SPP1489 days (say, June 2011, location to be decided).

1 Gröbner Bases for Arithmetic Geometry.

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Topics include:

**1** Gröbner Bases and syzygies over  $\mathbb{Z}$  and  $\mathbb{Z}/m\mathbb{Z}$ .

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- **2** Primary decomposition over  $\mathbb{Z}$  and  $\mathbb{Z}/m\mathbb{Z}$ .

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- **3** SAGBI bases over  $\mathbb{Z}$  and  $\mathbb{Z}/m\mathbb{Z}$ .

1 Syzygies and Free Resolutions.

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- 2 Schreyer and La Scala type algorithms in the non-commutative case.
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- 4 Implementations in the arithmetic case.

Modular Computations.

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Absolute Polynomial Factorization and Primary Decoposition.

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Topics include:

1 Adjust and implement new factorization algorithms.

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- 1 Adjust and implement new factorization algorithms.
- 2 Adjust and implement new absolute factorization algorithms.

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- 1 Adjust and implement new factorization algorithms.
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- 3 Absolute primary decomposition using various algorithms.

1 Tropical, Toric and Convex Geometry.

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#### Topics include:

- 1 Develop new data structures in SINGULAR for polyhedral computations.
- Develop software for the computation of tropical varieties.
- 3 Implement algorithms for toric geometry.

This requires closed cooperation with POLYMAKE and GFAN.

1 Cohomology and D-modules.

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Topics include:

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- 2 Implement Grothendieck's direct image process.

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- Implement Grothendieck's direct image process.
- Implement algorithms for deRham cohomology.

Numeric-Symbolic Methods for Solving and Primary Decomposition.

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#### Topics include:

- Link symbolic algorithms and numerical homotopy methods.
- 2 Speed up symbolic algorithms / certify numerical algorithms.

At current state this is based on a linkage of  $\operatorname{SINGULAR}$  and  $\operatorname{BERTINI}$ .

## Further Projects

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Other topics range from special algorithms for monomial ideals via parametrizing rational curves to implementing Böhm's tropical mirror construction.